Algorithms

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Recursion

- Topics:
 - Method call stack and activation records
 - Base case
 - Recursive case
 - Describe some recursive mathematical functions
 - Recursion and the method call stack
 - Describe when to use recursion

Today's Lecture

Activation Record (Stack Frame)

A record used at run time to store information about a function call, including the parameters, local variables, return address, and function return value (if a value-returning function)

Run-time Stack

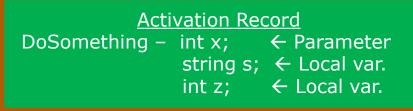
A data structure that keeps track of activation records during the execution of a program

How Recursion Works

- Variables and parameters are not just stored anywhere on the stack.
- Variables and parameters from the same function are grouped together on the call stack.

void doSomething(int x) {
 String s;
 int z;
 // other code here...

Activation Record Here is an activation record that would get created when doSomething is called.



Method Call Stack

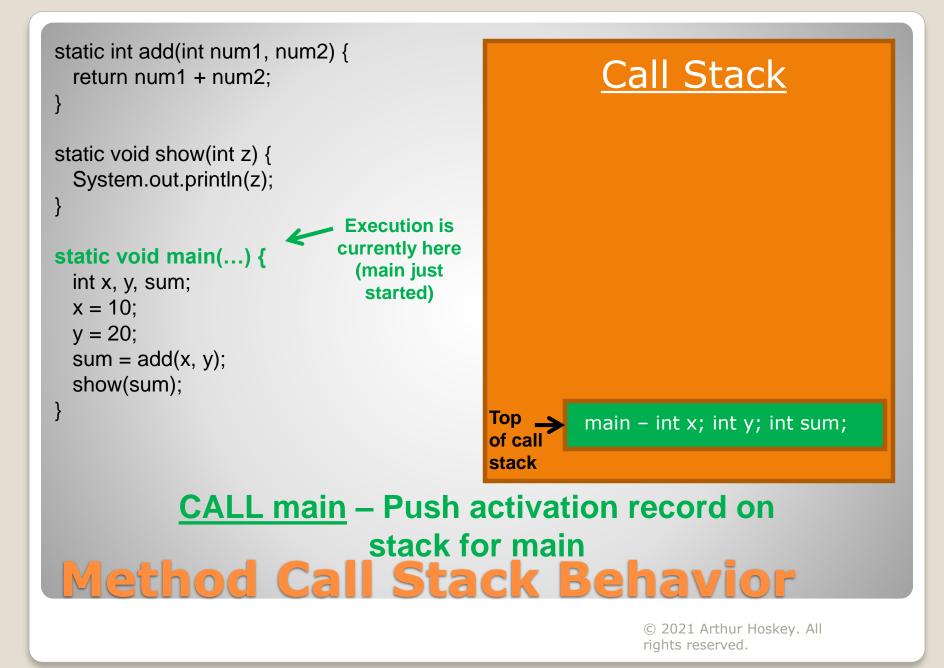
All variables declared in a function are stored in an activation record (or stack frame).

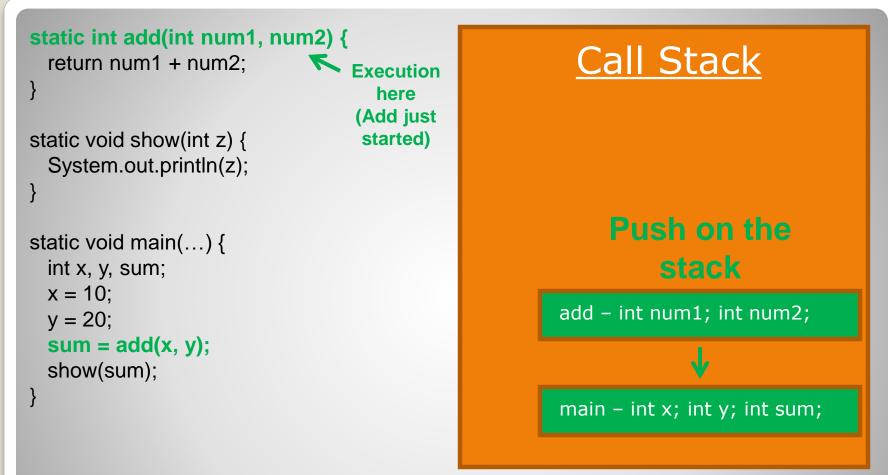
• The activation record for a function call stores all the variables and parameters declared in that function.

Activation Record Behavior

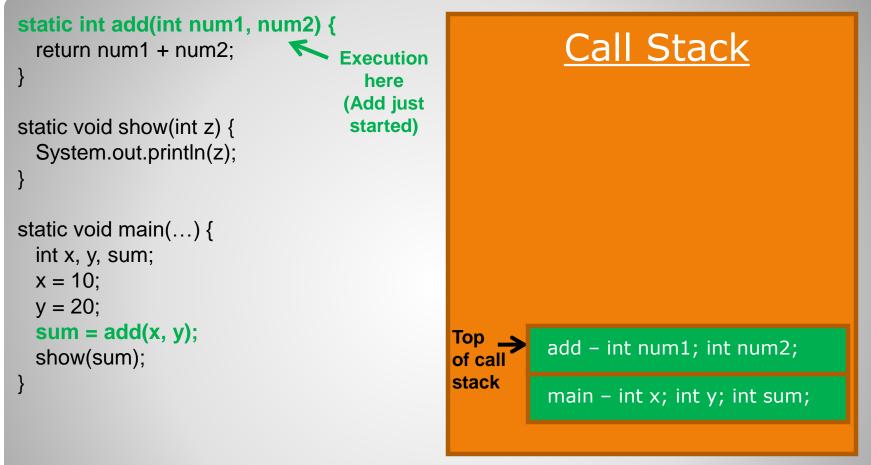
- Method call → Push new activation record on stack
- Method ends → Pop top activation record off stack

Method Call Stack

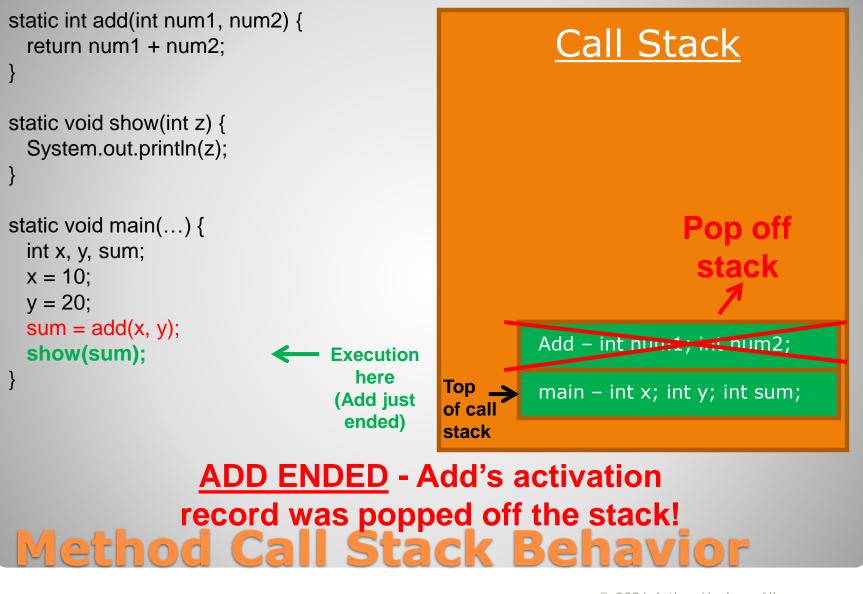


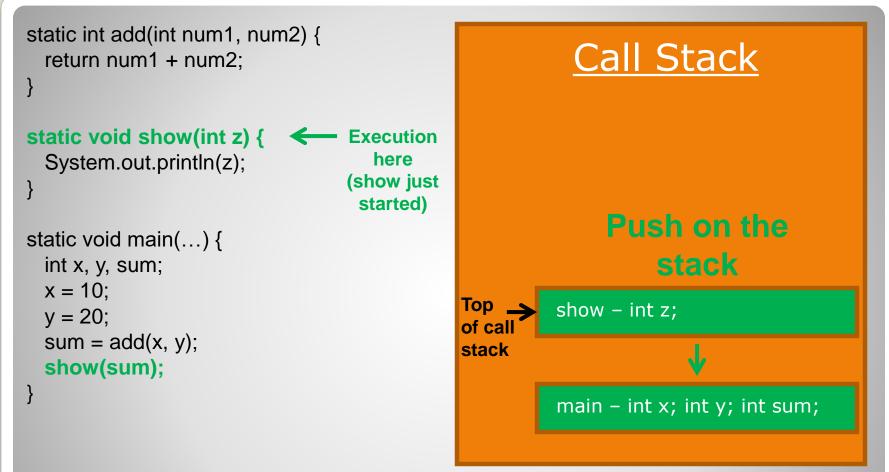


<u>CALL ADD</u> – Push activation record on stack for Add Method Call Stack Behavior

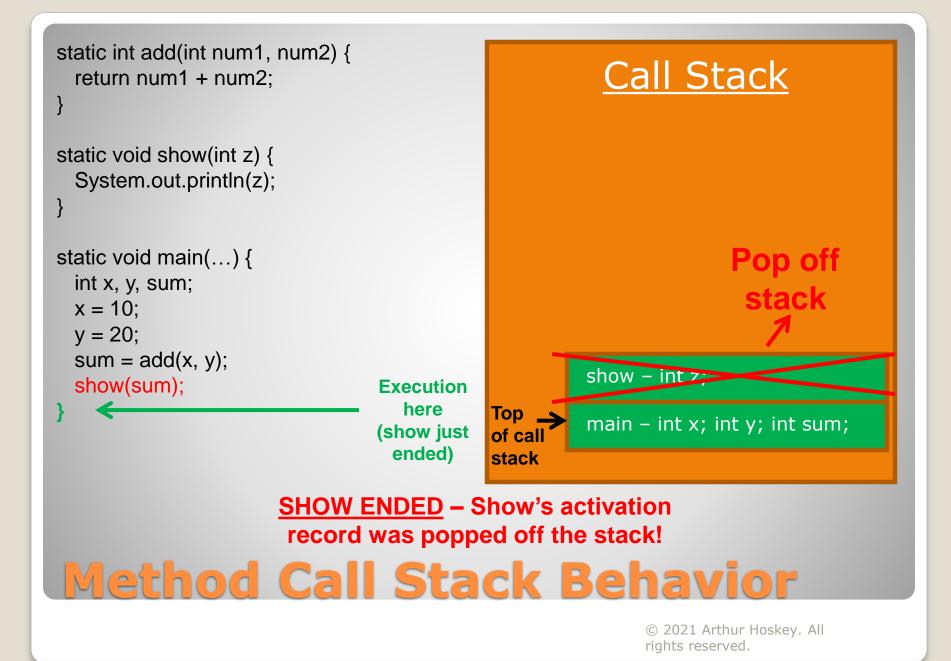


Add's activation record is now the top of the stack!!! Method Call Stack Behavior





CALL SHOW- Push activation record on stack for Show Method Call Stack Behavior



```
static int add(int num1, num2) {
                                                       Call Stack
 return num1 + num2;
static void show(int z) {
 System.out.println(z);
static void main(...) {
 int x, y, sum;
 x = 10;
                                                                     Pop off
 y = 20;
                                                                      stack
 sum = add(x, y);
 show(sum);
                                            Тор
                                                      main - int x int , int sum;
                                            of call
                                            stack
```

<u>MAIN ENDED</u> – main's activation record was popped off the stack! Program done.

Method Call Stack Behavior

Video

Recursion (Mario)

https://www.youtube.com/watch?v=fBJHeZgGQQ4



- Do the following tasks, given a recursive routine
 - Determine whether the routine halts
 - Determine the base case(s)
 - Determine the general case(s)
 - Determine what the routine does
 - Determine whether the routine is correct and, if it is not, correct it

Recursion Goals

- Do the following tasks, given a simple recursive problem
 - Determine the base case(s)
 - Determine the general case(s)
 - Design and code the solution as a recursive void or value-returning function
- Decide whether a recursive solution is appropriate for a problem

Recursion Goals

How is recursion like a set of Russian dolls?



What Is Recursion?

Recursive call

•A method call in which the method being called is the same as the one making the call

Direct recursion

Recursion in which a method directly calls itself

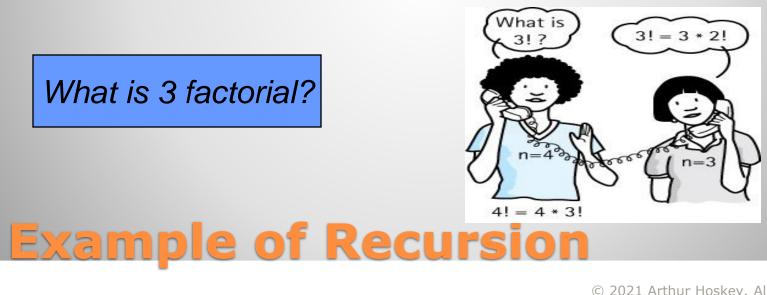
Indirect recursion

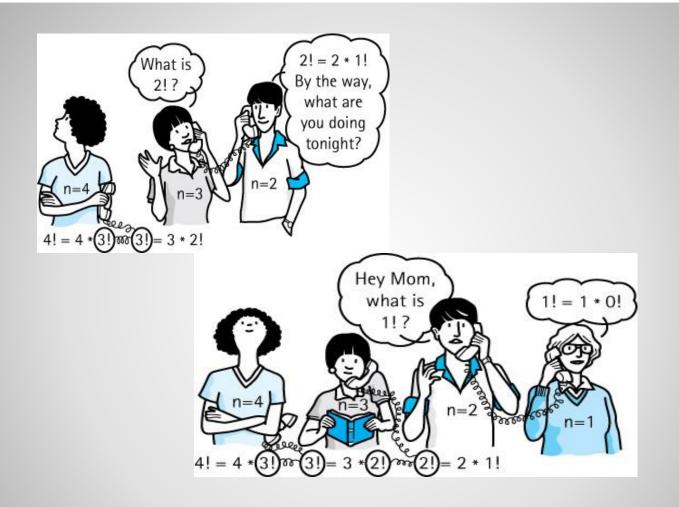
 Recursion in which a chain of two or more method calls returns to the method that originated the chain

What Is Recursion?

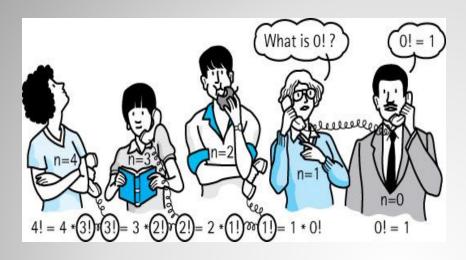
Recursive definition

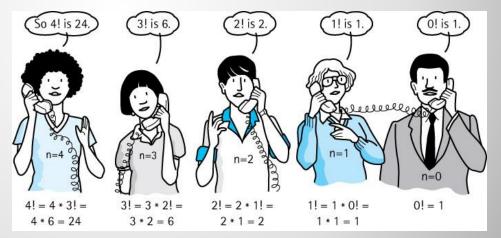
A definition in which something is defined in terms of a smaller version of itself



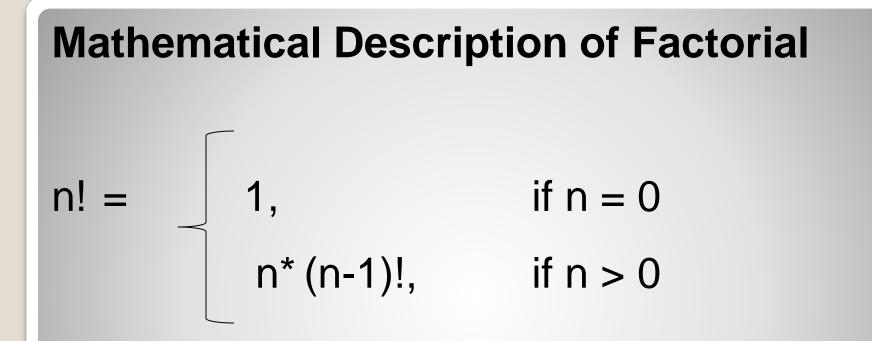


Example of Recursion





Examples of Recursion



Writing Recursive Solutions -Factorial

Base case

•The case for which the solution can be stated nonrecursively

•General (recursive) case

 The case for which the solution is expressed in terms of a smaller version of itself

Recursive algorithm

A solution that is expressed in terms of
 (a) a smaller instance(s) of itself and (b)
 a base case(s)

Example of Recursion

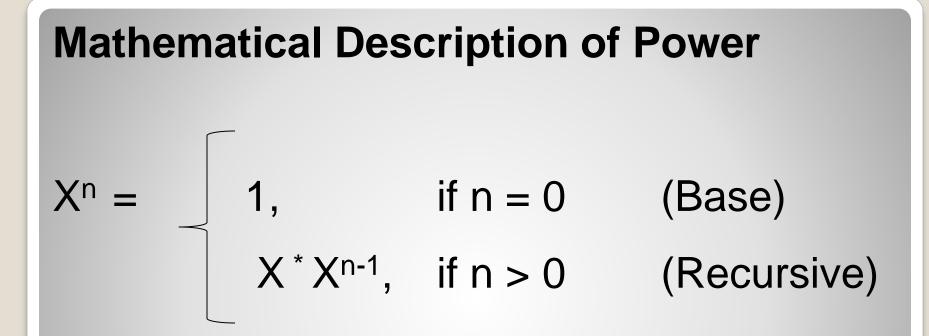
Algorithm for writing recursive solutions Determine the size of the problem Size is the factor that is getting smaller Size is usually a parameter to the problem Identify the **base case(s)** The case(s) for which you know the answer Identify the **general case(s)** The case(s) that can be expressed as a smaller version of the size

Writing Recursive Solutions

Let's try it

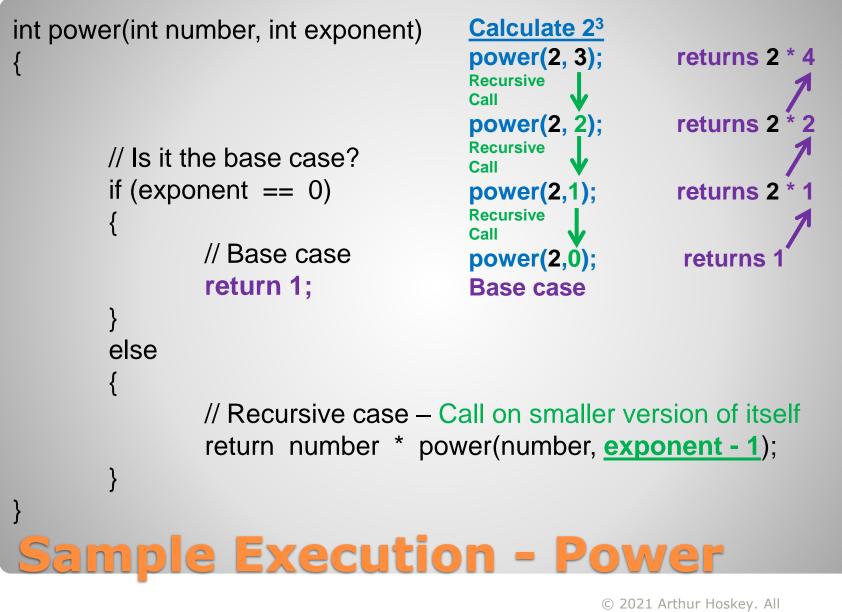
Problem: Calculate Xⁿ (X to the nth power) Recursive formulation: $X^{*}(X)^{*}(X^{n})^{*}...^{*}X$ (x n times) What is the size of the problem? Which case do you know the answer to? Which case can you express as a smaller version of the size?

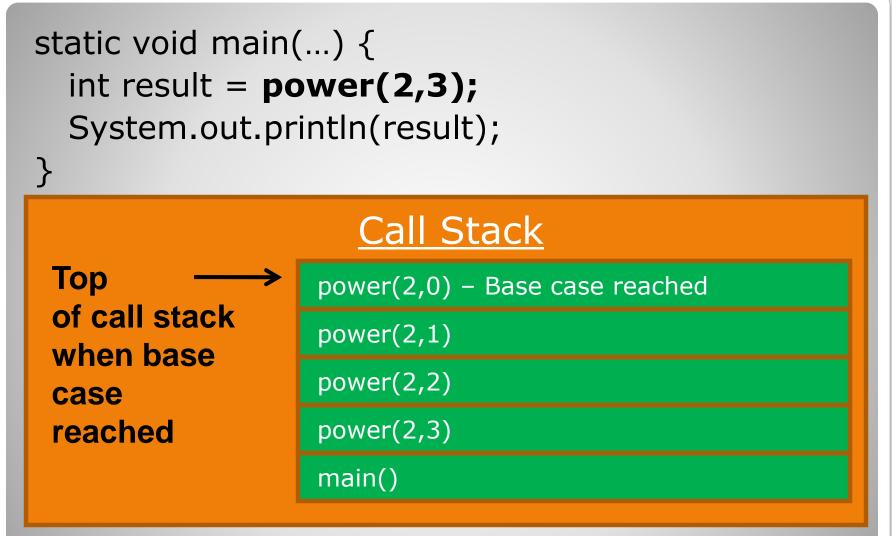
Writing Recursive Solutions -Power



Writing Recursive Solutions -Power

```
int power(int number, int exponent)
       // Is it the base case?
       if (exponent == 0)
              // Base case
              return 1;
                                              Problem is a smaller
                                               version of itself.
       else
              // Recursive case – Call on smaller case
              return number * power(number, exponent - 1);
Writing Recursive Solutions -
```





Sample Execution - Power

What would happen if we left out the base case?
 No base case in this method

// Recursive case – Call on smaller case
return number * power(number, exponent - 1);

Writing Recursive Solutions -Power

<pre>int power(int number, int exponent) { return number * power(number, exponent - 1); Stack Overflow!!! METHOD CALLS NEVER STOP!!!</pre>	
<u>Call Stack</u>	
<pre></pre>	 power(2,-2) power(2,-1) power(2,0) power(2,1) power(2,2) power(2,3) main()

Sample Execution – No base case

Pattern of solution

if (some condition for which answer is known) solution statement Base case

else

function call on smaller version of itself

Writing Recursive Solutions

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Recursive case

Shall we try it again? Problem: Calculate Nth item in Fibonacci sequence

0, 1, 1, 2, 3, 5, 8, 13, 21, 34, 55 What is the next number? What is the size of the problem? Which case do you know the answer to? Which case can you express as a smaller version of the size?

Writing Recursive Solutions -Fibonacci

Mathematical Description of Fibonacci Sequence

Fn = 0, if n = 0 1, if n = 1 Fn-1 + Fn-2, if n >= 2

Writing Recursive Solutions -Fibonacci

```
int fibonacci(int n)
{
    if (n == 0 || n == 1)
        return n;
    else
        return fibonacci(n-2) + fibonacci(n-1);
}
```

That was easy, but it is not very efficient. Why?

Writing Recursive Solutions -Fibonacci

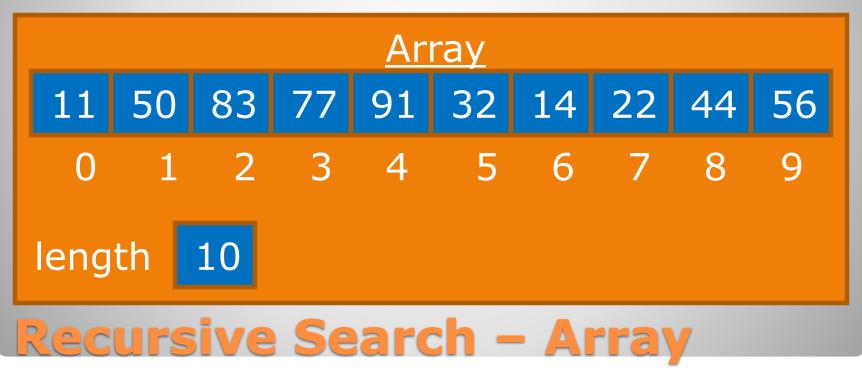
Shall we try it again?

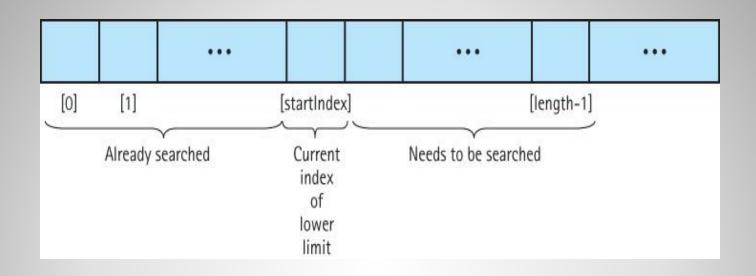
Problem: Search a list of integers for a value and return true if it is in the list and false otherwise.

Writing Recursive Solutions

Recursively search an array for an item.

Assume the following list:



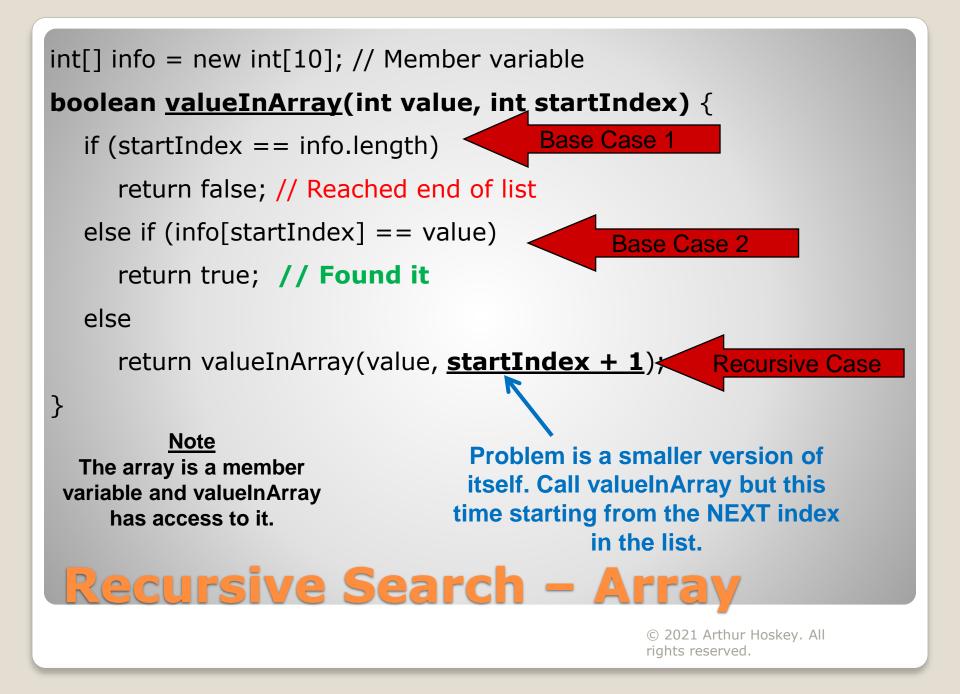


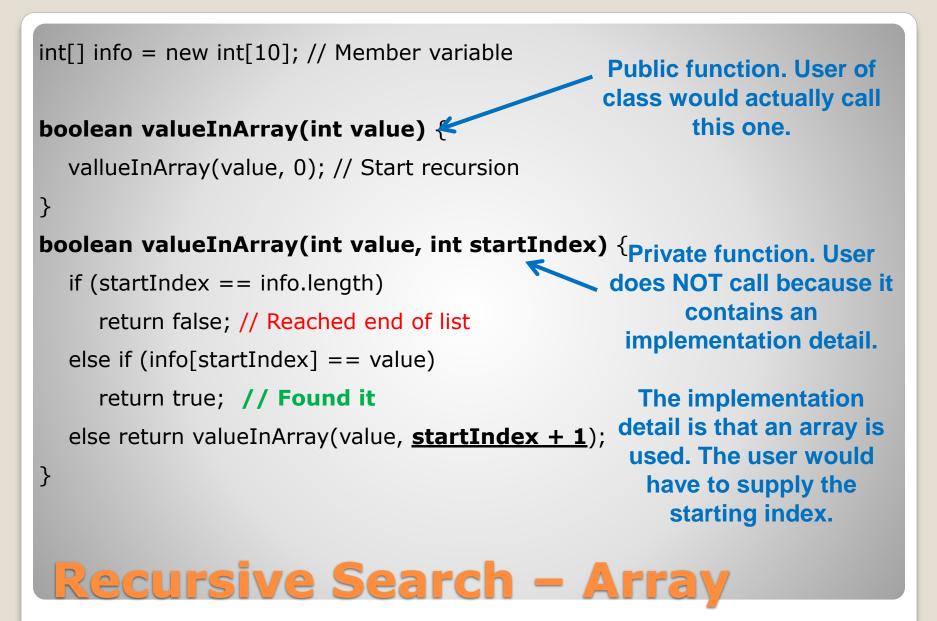
boolean valueInArray(int value, int startIndex);

Which case do you know the answer to?

Which case can you express as a smaller version of the size?

Recursive Search – Array





Why use recursion?

True, these examples could more easily be solved using iteration

However, a recursive solution is a natural solution in certain cases, especially when pointers are involved

Writing Recursive Solutions

Tail Recursion

The case in which a function contains only a single recursive invocation and it is the last statement to be executed in the function.

A tail recursive function can be replaced with iteration.

Stacking

Using a stack to keep track of each local environment, i.e., simulate the run-time stack .

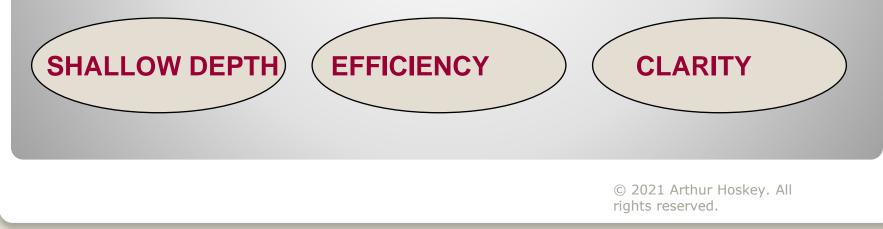
Removing Recursion

When To Use Recursion

•Depth of recursive calls is relatively "shallow" compared to the size of the problem

 Recursive version does about the same amount of work as the nonrecursive version (same Big-O)

•The recursive version is shorter and simpler than the nonrecursive solution



Recursion Real-time Speed

•The recursive version is generally slower than an equivalent iterative version.

•The reason the **recursive version** is slower is that it **generally requires more method calls**.

•Executing method calls is more time consuming than executing normal statements.



